The dynamics of clusters and groups of galaxies essentially depends on their masses. Unfortunately, the data available on the masses of galaxies are poor.

Observations of the orbital motions in double stars have been used to determine stellar masses. A great number of already determined orbits of visual and spectral doubles forms a sound basis for our knowledge of stellar masses. In contrast to this, we are in no position to determine the orbits in double galaxies, and attempts to make statistical use of the differences of radial velocities in double galaxies meet considerable difficulties in introducing this or that hypothesis on the nature of motion (elliptical or hyperbolic). What remains is to determine the masses of galaxies from measurements of rotation and of the internal motions within a given galaxy.

Unfortunately, the data obtained in this way accumulate very slowly. Thus the value commonly accepted at present for the mass of our Galaxy might very likely turn to be incorrect by a factor of 2. The estimate of the mass of the Large Magellanic Cloud is very uncertain. Our knowledge of the masses of both giant and dwarf elliptical galaxies is quite limited.

Nonetheless, the data available have made it possible to draw the following valuable conclusions as to the values of the ratio $f = M/L$.

(a) The ratio $f = M/L$ decreases at least 10 times when passing from the elliptical galaxies of high luminosity to the spirals and further to the irregular galaxies.

(b) The ratio $f$ does not increase but, most probably, decreases when passing from supergiant elliptical galaxies via giants to the dwarf systems like those in Fornax and Sculptor.

As a result, the ratio of the masses, say, of the supergiant and the dwarf galaxies, turns out to be larger than the ratio of their luminosities.

For instance, the supergiant elliptical galaxy NGC4889 in the Coma cluster surpasses in luminosity the dwarf system discovered in Capricorn by Zwicky, by nearly one million times and the ratio of the masses is probably much larger.

Quite different is the picture in the case of stars where luminosity increases in proportion to a rather high power of the mass. This accounts for the fact that although the luminosity of stars can vary by hundreds of millions of times, their masses vary at most by about a thousand times and most of the stars have masses differing from the average by not more than a few times.

As a consequence, the gravity field in any stellar cluster is determined almost equally by the bright as well as by faint members of the cluster. With clusters and groups of galaxies the situation is different. Here the dwarf galaxies have almost no influence upon the structure of the gravity field, which is determined chiefly by a small number of supergiants and partly by the giant galaxies.

Zwicky (1957) has rendered great service proving the monotonic increase of the number of galaxies with decrease of luminosity (the monotonic form of the luminosity function). Probably, such an increase takes place in the majority of clusters and groups of galaxies. However, even
relatively large number of low-luminosity galaxies produce negligible influence upon the structure of the field of gravitation inside and outside the cluster. Suffice it to say that in the Local Group the total mass as well as the gravity field are determined mainly by two members — M31 and our Galaxy.

This circumstance can simplify a number of problems on the dynamics of clusters of galaxies, for we can consider only a small number of its massive members.

We observe multiple galaxies in great numbers. The question of the type of configuration of these systems can be raised as was the case with multiple stars. Division of all configurations into two types seems suitable: common configurations and configurations of the trapezium type. The latter include multiple systems in which at least three members can be found having mutual distances of the same order of magnitude. These configurations cannot be stable and they disintegrate within a period of the order of several revolutions in the system.

The observations indicate that in real stellar systems of the trapezium type one of the components belongs to $O$ or $B$ spectral types. Such stars are of recent formation and for them the number of revolutions in the system is expected to be small. However, the observations show that a few multiple stars of later spectral classes also possess trapezium-like configurations. Of course, the configurations we observe are projections of true space configurations. Therefore, even if there are no real trapezium configurations of later-type stars, a small percentage ($\sim 8\%$) of apparent configurations of the trapezium type will appear due to projection. This is almost precisely the percentage of trapezium configurations observed in cases where the components of multiple stars do not belong to the $O$ and $B$ spectral types. In other words, there are no or almost no real configurations of the trapezium type among the late-type multiple stars.

Quite reverse is the case with multiple galaxies. As pointed out in (Ambartsumian 1956), out of the 132 multiple galaxies, in Holmberg’s catalogue of the double and multiple galaxies (Holmberg 1937), 87 have configurations which should, doubtless, be classed trapezium type. Thus, systems of galaxies of trapezium type are markedly dominant, and most of the multiple galaxies are of recent formation; i.e., their components could have made but a few revolutions from the moment of formation of the system.

Two remarks are to be made in this connections: (1) The period of revolution in the multiple and double galaxies should be of the order of $10^9$ years. Therefore, the age of the multiple systems we have observed could possibly be $5 \times 10^9$ years or more. In the sense of instability of multiple systems, the galaxies are probably young, although their age can in some cases be three or four times more than $5 \times 10^9$ years. (2) The instability of trapezium configurations has not yet received a clear-cut mathematical treatment. However, simple considerations make it evident that the above-mentioned time of dissolution (several periods of revolution) holds true only for cases where the masses of all three components on which the trapezium configuration is based are of the same order of magnitude; otherwise the system can exist considerably longer. Furthermore, the components must be of comparable luminosity. A substantial number of the observed multiple galaxies in fact meets this requirement. In particular, in such systems as Stephan’s Quintet and Seyfert’s Sextet.
the differences in stellar magnitudes are comparatively small. By contrast, trapezium configurations where one of the components is much brighter than the others (for example, the system $M_{31}$, $M_{32}$ and NGC205) are, presumably, much more stable.

On the other hand, there are cases where in a cluster of galaxies three or four members which are noticeably brighter than all the rest (and therefore contain the greater part of the mass) and together form a trapezium configuration. Considering only the interaction of these brighter galaxies, it can be asserted that such systems should be unstable. For example, the four galaxies NGC3681, 3684, 3686, and 3691 form a typical multiple system of the trapezium type; at least a dozen other much fainter galaxies are included in this system, but the system is evidently unstable. The galaxies $NGC_{7383} - 7390$ belong to a small cluster containing six bright members and more than a dozen faint components. The bright members constitute a trapezium–type system. Finally, the three galaxies, NGC3613, 3619 and 3625, form a small group containing at least eight fainter objects. In this case there are fainter objects of considerable angular diameters and low surface luminosity. Again we have an unstable group, although this group is not, apparently, a cluster of its own, but forms a condensation in the Ursa Major Cloud.

The arguments put forth in our previous papers speak in favor of the joint formation of the members of each cluster or physical group of galaxies. We refrain from repeating these arguments, but because we still encounter published assertions as to the possibility of formation of groups and clusters of galaxies from independent members of the general metagalactic field, a new argument will be advanced. This is based on the existence of systems consisting of a few very bright galaxies and a larger number of faint members. In principle, it is possible to understand the dynamical formation of one physical pair by the accidental encounter of three galaxies. Generally speaking, this pair in the course of time can capture other galaxies too. However, the exchange of large amounts of energy must take place between the interacting galaxies, and to achieve this end the interacting galaxies must have masses of about the same order. Let us assume that a multiple system of three or more massive galaxies has come into being in this manner (although this can be proved to be highly improbable). No galaxy of an essentially small mass (say by two orders less) can ever be captured by such a group, because the exchange of kinetic energies in the case of large mass ratio is always negligibly small. Thus, the mechanism of capture meets with new difficulties in any attempt to account for the existence of galaxies of small mass in groups and clusters. This difficulty applies to all three of the above examples of multiple systems of bright galaxies with an additional number of fainter members, and also to the case of a pair of bright galaxies NGC521, 533, which has a number of very faint companions.

The great difference in distribution of bright and faint members is most apparent in the large spherical clusters of galaxies. The bright members are densely concentrated, while the faint ones occur relatively more frequently on the periphery. This phenomenon was given special consideration by Zwicky, who showed that the Coma cluster is of very large dimensions if we judge from the distribution of galaxies of low luminosity. However, the case is completely different with irregular clusters. According to Reaves (1956), faint galaxies of low surface luminosity in the Virgo cluster
reveal approximately the same distribution and, consequently, the same degree of concentration as bright galaxies.

Such a picture occurs also in the case of the objects of low surface brightness and small density gradient in the well-known cluster in Fornax. As Hodge points out (1959), the search for similar objects in regions neighboring the cluster has led to negative results. Finally, in the above-mentioned case of NGC3613, 3619 and 3625, galaxies of low surface brightness and low luminosity do not spread far beyond the bounds determined by the group of bright galaxies.

These examples bear testimony to the fact that equipartition of energies between the bright and the faint members of the irregular clusters is out of the question, and that the phenomena of instability are expressed in irregular clusters much more sharply than in the spherical ones.

The existence of a great number of trapezium configurations signifies that many of the multiple galaxies are unstable formations. If this is the case, we have no right to assume a priori that the multiple galaxies should be negative-energy systems. In the case of simple double stars (we exclude O and B stars) it could be asserted without any knowledge of their orbits that, for the most part, they have negative total energies. In fact, if the majority of the multiple stars had positive total energy then the time of disintegration could be only a few tens of thousands of years, and within such a period most of the multiple stars would be replaced by stars of a new generation. In other words, positive total energy would lead to an erroneous conclusion about the rate at which stars are formed in the Galaxy.

Yet in the case of multiple galaxies the assumption of positive total energy for most of them does not lead to similar erroneous deduction. The age of the component galaxies derived in this way is but a few times less than that accepted for our Galaxy. Therefore we infer that the sign of the energy of the multiple galaxies, groups and clusters of galaxies should be determined in each case, relying upon observational data.

The reasons put forth above support the view that the a priori assumption of positive total energy in a number of systems of galaxies cannot be regarded as more audacious than, say, the assumption that almost all such systems possess negative energy. Nevertheless, let us consider the facts: For a number of multiple systems the negative total energy assumption implies that the ratio $f = M/L$ must be about one order of magnitude larger than what follows from other data. Thus it is pointed out by Kalloghjan that the multiple system comprising NGC68, 69, 71, 72 and one anonymous galaxy, if it has negative total energy, would lead to a value of $f$ greater than 300. For the double galaxy NGC7385−7386, he finds $f$ greater than 600.

The sign of total energy of Stephan’s Quintet has been determined by us and by G. and E. M. Burbidges (1959), resulting in positive total energy. Later, Limber and Mathews (1960) indicated that, under certain assumptions, when the mass of the components is supposed to be very high, the Quintet can have a negative total energy.

The sign of the total energy in a number of clusters of galaxies is elucidated in several recent investigations in detail. A number of difficulties are caused by uncertainty in the exact value of $f$ for giant elliptical galaxies. This value is believed to lie in the range $30 < f < 70$. However,
greater values \((f \sim 100)\), although rare, are not excluded, particularly for the brightest supergiants \((M \sim -21.5)\). No straightforward data exist that would enable us to estimate the value of \(f\) for these brightest supergiants. It is natural, therefore, to believe that the sign of the total energy is determined with greater reliability in those clusters and systems in which there are no supergiant elliptical galaxies. The case will be even better for systems with no giant elliptical galaxies either, and that is why the positive total energy of the nearby system of galaxies in Sculptor, as established by de Vaucouleurs (1959) is of paramount importance.

Of no lesser value is the result obtained by van den Bergh (1960) in respect to the cluster of galaxies in Canis Venatici, although studies toward determining the borders and identifying the members of this cluster should continue.

The Hercules cluster, investigated by G. and E. M. Burbidges (1959), contains but a small percentage of bright elliptical galaxies. To admit negative total energy of this cluster we have to ascribe to \(f_E\) the value of order of 300, which seems to be improbable. The contrast becomes still sharper in the case of the cluster in Virgo. Assuming the stability of this system we should have to acknowledge that \(f_E > 1000\), as shown by de Vaucouleurs (1960).

It might be conjectured that perhaps the Coma cluster could have negative total energy if the modern distance scale of Sandage could be further changed by further diminution of the redshift constant. On the other hand, many members of this cluster are elliptical galaxies of moderate luminosity. The value \(f\) cannot be very high for them, so that a particularly high value of \(f\) must be ascribed to the remaining supergiant galaxies if the cluster has negative total energy.

Naturally, the sharp discrepancy between the summed luminosities of the clusters of galaxies and the masses found by applying the virial theorem has compelled some authors to favor the hypothesis of supplementary masses in the clusters which do not form part of member galaxies, i.e., intergalactic matter. Yet the data available on the upper limit of opacity in the clusters of galaxies, as well as the data on the 21–cm radiation, are not favorable.

There remains the assumption of a comparatively rich intergalactic stellar population in the clusters. Such a possibility has been contemplated in detail by de Vaucouleurs with reference to the Coma cluster. The result is negative if we refrain from an improbably large value of \(f\) for this intergalactic stellar population. This result apparently refers to other clusters as well.

Thus there is only one natural assumption left relating to the clusters cited above—they have positive total energies. It should be stressed that no \textit{a priori} arguments can be advanced against this assumption.

A study of the structure of the irregular clusters of galaxies leads one to the conclusion that often they are made up of several superimposed groupings. An interesting example of such a grouping was pointed out by Markarian a few years ago: the chain of bright galaxies in the Virgo cluster containing \(NGC\)4374, 4406, 4438 and others. This wonderful arc of eight bright galaxies is presumed to represent a physical grouping within the Virgo cluster. On the other hand, facts about the radial velocities of the members of this group undoubtedly establish its positive total energy.

Recently I looked through the abstract of van den Bergh’s latest paper, in which an assumption
of irregular clusters consist of separate subsystems and subclusters is made in the most general form. It is difficult to overestimate the importance of this phenomenon in comprehending the evolution of clusters of galaxies. In this case we apparently have consecutive formation of relatively independent subsystems (subclusters), the superposition of which brings about irregular clusters. It is probable that many of these subsystems have a positive total internal energy.

Of considerable interest are the results of determination of the average value of \( f \) from the differences of radial velocities in double galaxies as obtained by Page (1961), who obtained for spiral and irregular galaxies \( f = 1/3 \); for ellipticals and lenticulars \( f = 94 \). These values are derived on the assumption that in double galaxies the motion takes place in circular orbits. The value of \( f \) for spiral and irregular galaxies is even less than the value derived from rotations of single galaxies. This means that all or almost all of the observable narrow pairs of such galaxies constitute negative energy systems. Let us compare this with the unusually large values of \( f \) obtained on the basis of the virial theorem for clusters composed of spiral and irregular galaxies. The comparison leads to two inevitable conclusions:

(a) All explanations allowing for the negative total energy of clusters and groups made up of spirals and irregular galaxies become still more highly improbable, since the arguments adduced in similar cases are likewise applicable to the double galaxies.

(b) There are almost no systems with positive energy among the isolated double galaxies, for such systems can represent a narrow pair only for a very short duration of time (of the order of \( 10^8 \) years).

If this is so, then the double elliptical systems should also be regarded as systems possessing, for the most part, negative energies, and Page’s value \( f = 94 \) can be taken as close to the real value. This brings us nearer to the conclusion about negative total energy of the Coma cluster.

It is interesting to note that when we pass from double galaxies to multiple configurations of the trapezium type, the differences of the velocities of the components become much greater. For these configurations negative total energy assumption leads to too large values of \( f_E \).

Speaking of instability in systems of galaxies, we should also touch upon the radio galaxies which, as a rule, occur in clusters of galaxies. Apparently the radio galaxies are always among the few brightest members of the corresponding clusters. The best example is furnished by the source Perseus A (NGC1275), which is the brightest member of the cluster in Perseus.

In the radio galaxy NGC4486, a jet is being ejected from the central nucleus with separate condensations, the luminosities of which resemble those of dwarf galaxies. Apparently these condensations contain an enormous amount of relativistic electrons. However, it is difficult to refute the suggestion that these condensations include also a substantial amount of common matter in addition to the relativistic plasma. In particular they are likely to contain sources of relativistic electrons.

A strong argument in support of this view is provided by the galaxies NGC3651 and IC1182 whose nuclei eject jets containing blue condensations. These galaxies with blue jets are also among the brightest members in the corresponding clusters. Finally, there are cases when blue components occur in the vicinity of other giant elliptical galaxies, which evidently represent a later stage in the
evolution of the above blue condensations.

In all probability, the condensations in NGC4486 represent an earlier stage of evolution of the same objects. In such cases the intensity of radio emission of the blue condensations and the blue companions is believed to have already weakened.

As revealed in Byurakan, a blue object of photographic magnitude 18.5 is situated very close to the remote radio galaxy in Hydra. The color index of this object is about –0.5. Since its diameter is less than 2000 parsecs on our plates it looks like a star. If it can be shown that this object is in fact a physical companion of Hydra A, then a close connection between the two types of eruptive activities of the nuclei of supergiant galaxies will be established: ejection of plasma condensations and ejection of blue condensations. One way or another, all the data indicate that this activity is of great import in the origin of galaxies.

We conclude that there exist clusters which are in a particularly active phase of evolution when new galaxies originate within them. The existence of a radio galaxy is an indicator of this phase. It is possible that in such a phase the radio emission erupts now and then with varying intensity.

In the ratio galaxy Perseus A it large relative velocities are observed, up to 3000 km/sec. Such velocities exceed the velocity of escape from the cluster and thus speak for themselves of instability.

It seems, therefore, that a study of the ratio galaxies as systems from whose nuclei large masses are ejected or which are in the process of division must throw new light upon the phenomena of instability in the clusters of galaxies.

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